Network-Aware Search in Collaborative Tagging Applications: Instance Optimality versus Efficiency

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A Web of social interactions

Social Web: new development to the Web – users, their relationship and their data.

Significant and highly qualitative portion of the Web:
- either built as explicitly social (Facebook, Google+, Twitter), or
- content-based, but with social communities acting as “engine” (Wikipedia, blogs, forums) - implicitly social

Larger user bases $\leadsto$ better search models for data relevance, freshness guarantees.
The social tagging context

**Collaborative tagging networks**: a good abstraction of social Web applications

- users form a social network (may reflect proximity, similarity, friendship, closeness, etc)
- user **tag items** (e.g., documents, URLs, photos, etc) from a public pool of items
  - examples: Flickr, Delicious, Netflix, Youtube, even Twitter

Users search for items having certain tags
Outline

Problem definition

Solution

Approximation algorithms

Experiments
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The social tagging context

Setting: a collaborative tagging environment in which we have:
  ▶ set of items $I$, set of users $U$, set of tags $T$.
  ▶ tagging relation: Tagged(user, item, tag)

Social Network: undirected weighted graph $G = (U, E, \sigma)$
  ▶ nodes represent users
  ▶ $\sigma$ associates to each edge $e = (u_1, u_2)$ a value in $(0, 1]$ called the proximity between $u_1$ and $u_2$ (a social score)
The top-k retrieval problem

Problem (Top-k retrieval)

*Given a seeker* $s$, a query $Q = \{t_1, \ldots, t_r\}$ (a set of $r$ distinct tags), an integer value $k$, and an item scoring model, retrieve the top-$k$ items

- main challenge: efficiency and applicability

Difference to classical search: item scores depend on its taggers and their proximity to the seeker
Scenario: Alice wants top-2 documents for query \{news, site\}

\[ \rightarrow \text{result we desire is } D4, D2 \]
What would happen in classical search?

each tag has same weight in **term-frequency** lists; TA/NRA

[Fagin01]

<table>
<thead>
<tr>
<th>news</th>
<th>site</th>
</tr>
</thead>
<tbody>
<tr>
<td>doc</td>
<td>tf</td>
</tr>
<tr>
<td>D4</td>
<td>2.00</td>
</tr>
<tr>
<td>D3</td>
<td>1.00</td>
</tr>
<tr>
<td>D5</td>
<td>1.00</td>
</tr>
<tr>
<td>D2</td>
<td>1.00</td>
</tr>
<tr>
<td>D1</td>
<td>1.00</td>
</tr>
</tbody>
</table>

Bob, Charlie, Ed
What would happen in classical search?

Each tag has the same weight in term-frequency lists; TA/NRA [Fagin01]

⟹ top-2 result: D4, D3
Social frequency

Classic term frequency is replaced by a monotonic measure depending on the seeker and a parameter $\alpha$:

$$fr(i \mid u, t) = \alpha \times tf(t, i) + (1 - \alpha) \times sf(i \mid u, t)$$

$sf(i \mid u, t)$ represents the social frequency:

$$sf(i \mid u, t) = \sum_{v \in \{v \mid Tagged(v, i, t)\}} \sigma(u, v)$$

The extreme cases:

- $\alpha = 1$ classical search
- $\alpha = 0$ exclusively social search
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The scoring model

\( score(i \mid u, t) \) is the score of item \( i \) for the given seeker \( u \) and tag \( t \): e.g., \textit{tf-idf}: \( score(i \mid u, t) = fr(i \mid u, t) \times idf(t) \), BM25

\( score(i \mid u, Q) \) is the overall score of \( i \) for seeker \( u \) and query \( Q \): e.g., monotone aggregation functions: \textit{sum, max, avg}
Considering only direct connections

scores depend on proximity: per-seeker lists [Amer-Yahia08]
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\( \therefore \) top-2 result: D5, D3
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Adding indirect connections

indirectly connected users should be relevant too

e.g., Danny might be more similar to Alice than Charlie
Extended proximity ($\sigma^+$): we want to compute a social score even for users that are not directly connected to $s$.

\[
sf(i \mid u, t) = \sum_{v \in \{v \mid Tagged(v, i, t)\}} \sigma^+(u, v)
\]
Possible definitions for $\sigma^+$

On a path, $p = (u_1, \ldots, u_l)$, monotonically aggregate the weights:

▶ Example 1: path multiplication $\sigma^+(p) = \prod_i \sigma(u_i, u_{i+1})$

▶ Example 2: minimum value on a path
  $\sigma^+(p) = \min\{\sigma(u_i, u_{i+1})\}$

▶ Example 3: exponential decay $\sigma^+(p) = \lambda^{-\sum_i \frac{1}{\sigma(u_i, u_{i+1})}}, \lambda \geq 1$

Then choose the optimal of the aggregated paths:

$$\sigma^+(s, u) = \max_p\{\sigma^+(p) \mid s \xrightarrow{p} u\}.$$
Considering indirect connections

per-seeker proximity lists

<table>
<thead>
<tr>
<th>user</th>
<th>prox.</th>
</tr>
</thead>
<tbody>
<tr>
<td>Bob</td>
<td>0.90</td>
</tr>
<tr>
<td>Danny</td>
<td>0.9x0.9</td>
</tr>
<tr>
<td>Charlie</td>
<td>0.60</td>
</tr>
<tr>
<td>Ed</td>
<td>0.6x0.5</td>
</tr>
</tbody>
</table>
Considering indirect connections

per-seeker proximity lists
⇝ top-2 results: D4, D2
**Our goal:** early-termination algorithm, in the style of TA/NRA: inverted lists of $tf$ values, and **proximity** lists are accessed sequentially.

Key subroutine: getting the next closest user

- pointer increment in the user proximity lists
Previous approach: **CONTEXTMERGE** [Schenkel08] - precomputed proximities for all user pairs.

**Major drawbacks:**

- **high disk space cost:** $\sim$ 700 TB for Delicious, even bigger for Facebook
- **limited applicability:** social scores can evolve (e.g., tag similarity), lists need to be kept up to date
Observation
The visit of the network in decreasing order of proximity (w.r.t the seeker) can be done on the fly and as needed
▶ for a wide family of $\sigma^+$ functions - monotone functions (including the 3 examples)
Our contribution: the SNS algorithm

Observation
The visit of the network in decreasing order of proximity (w.r.t the seeker) can be done on the fly and as needed
  ▶ for a wide family of $\sigma^+$ functions - monotone functions (including the 3 examples)

Advantages:
  ▶ a typical network can easily fit in main-memory
  ▶ spare the potentially huge disk volumes required previously
  ▶ social score updates become a non-issue
  ▶ full personalization: each seeker can choose any function
Computing the proximities

The previous three $\sigma^+$ examples satisfy the following property (Descending monotonicity):

Property

*Given a social network $G$ and a seeker user $s$, for any other user $v$ in $G$ that is connected to $s$ we have $\sigma^+(s, v) \geq \sigma^+(s, v\text{.previous})$.*

$\Rightarrow$ the proximities for a given seeker can be greedily computed on the fly - by generalizing Dijkstra’s algorithm.
Formal guarantees: correctness

Property
SNS visits the users of the network in decreasing order of their $\sigma^+$ values with respect to the seeker.

Corollary
SNS visits the users who may be relevant for a query in the same order as ContextMerge (or equivalent algorithms) and hence outputs equivalent results.
Formal guarantees: instance optimality

**Theorem**

$SNS_{\alpha=0}$ *is instance optimal* over all algorithms that do not make “wild guesses” and over all inputs $D$, when $\text{cost}(A, D) = \text{users}(A, D)$.
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Experiments
Is instance optimality enough?

No, at least in most practical scenarios

Two main reasons:

- the search may visit a significant part of the network, yet the final top-$k$ is established relatively soon,
- computing exact shortest paths, even in an optimal manner, still has a significant execution overhead.
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Possible directions:
1. tighter bounds for the termination condition, by estimating unseen proximities,
2. estimate all user proximities, via approx. shortest paths.
Approximations - estimating score bounds

Termination conditions too weak in practice, values drop rapidly:

\[ \Rightarrow \text{having a high-level description of the proximities, can lead to tighter score estimations but approximate results} \]
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Two approaches for estimation using a probabilistic parameter \( \delta \):
1. storing high level statistics, mean and variance (SNS/MV)
2. storing histograms of the proximity vectors (SNS/H)
Approximations - estimating user proximities SNS/L

Adaptation of the landmarks approach of [Potamias09]:

- for a number of $d$ landmarks, compute the entire proximity vector
- by triangle inequality, we can obtain upper and lower bounds of any seeker, user pair:

$$\min\left(\frac{\sigma^+(s, l_i)}{\sigma^+(l_i, v)}, \frac{\sigma^+(l_i, v)}{\sigma^+(s, l_i)}\right) \geq \sigma^+(s, v) \geq \sigma^+(s, l_i) \times \sigma^+(l_i, v)$$

- by accessing sorted landmark lists à la TA we can estimate user proximities without needing expensive priority queues.
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## Experiments: datasets

<table>
<thead>
<tr>
<th>Statistic</th>
<th>Delicious</th>
<th>Twitter</th>
</tr>
</thead>
<tbody>
<tr>
<td>users</td>
<td>80,000</td>
<td>570,387</td>
</tr>
<tr>
<td>items</td>
<td>595,811</td>
<td>1,570,866</td>
</tr>
<tr>
<td>tags</td>
<td>198,080</td>
<td>305,361</td>
</tr>
<tr>
<td>((u, i, t)) triples</td>
<td>2,863,365</td>
<td>8,753,706</td>
</tr>
<tr>
<td>distinct items/user</td>
<td>9.59</td>
<td>10.10</td>
</tr>
<tr>
<td>distinct tags/item</td>
<td>4.22</td>
<td>1.39</td>
</tr>
<tr>
<td>distinct tags/user</td>
<td>15.64</td>
<td>9.45</td>
</tr>
</tbody>
</table>

For experiments, three pairwise similarity networks (tag, item, and item-tag)
Experiments: performance

- - - ContextMerge  ---  SNS  ---  SNS/MV  ---  SNS/H  ---  SNS/L

- significant gains in performance, for both exact and approximate approaches
Experiments: precision/speed tradeoff

- high precision even when using simple statistics and independence assumptions
What / when?

- **exact approach**: very sparse network, very low proximity values, in cases where access is limited (e.g., Web API requests), relatively low $k$,

- **histograms/bounds approach**: sparse network and low proximity values, high $k$,

- **landmarks approach**: denser networks with (relatively) high proximity values, high $k$. 
To summarize

- novel algorithm generalizing shortest path based social search
- instance optimal in the exclusively social case for monotonic proximity functions,
- approximate approaches can be added to the framework, for further efficiency

Thank you.
SNS_{\alpha=0} (general flow)

Require: seeker s, query Q = (t_1, \ldots, t_r)
initialization of the distances and max-priority queue H
candidate list D = \emptyset, seeker s entered to queue H
while exists an user u in the queue H do
  compute \sigma^+(s, u)
  get all documents d belonging to u, tagged with t \in Q
  compute their scores and insert them into D
  prune the heads of the lists IL, removing documents in D
  refine (or relax) the proximity scores for neighbours of u from G
  if MinScore(D[k], q) \geq \max_{l>k}(MaxScore(D[l], q)) and
    MinScore(D[k], q) \geq MaxScoreUnseen
    then break
  end if
end while
return D[1], \ldots, D[k]
performance gains increase with network size, gains relatively constant with $k$
Experiments: relevance

- social keyword queries can provide good prediction accuracy for bookmarking